



## Summary

- PEVD of eigenbeams for speech enhancement performs identically and sometimes better than Raw PEVD [1] at a fraction of its complexity factor
- Effective for speech enhancement in noisy, reverberant environments
- No noticeable artifacts, blind and unsupervised approach
- Robust even when eigenbeams are not steered towards the speaker
- Listening examples are available at [2]

## Multi-channel Signal Model

Incorporating the reverberant channel model  $\mathbf{h}_q$ , the  $q$ -th microphone signal on a spherical array is

$$x_q(n, \mathbf{r}_q) = \mathbf{h}_q^T \mathbf{s}_0(n) + v_q(n) = \tilde{s}_q(n) + \tilde{v}_q(n),$$

where  $s_0(n)$ : clean speech,  $v_q(n)$ : noise signal,  
 $\mathbf{r}_q = (r, \theta_q, \phi_q)$ ,  $r$ : radius,  $\theta_q$ : elevation,  $\phi$ : azimuth

## Spherical Harmonic Decomposition

Spherical harmonic (SH) transform of the spatially sampled sound field:

$$\chi_\ell^m(n) \approx \sum_{q=1}^Q \alpha_q x(n, \mathbf{r}_q) R_\ell^m(\mathbf{r}_q)$$

$\alpha_q$ : quadrature weights,  
 $L$ : max. SH order,  
 $\mathcal{L} = (L+1)^2$  eigenbeams,  
 $R_\ell^m(\mathbf{r}_q)$ :  $\ell$ -th order,  $m$ -th degree real SH basis

Arranging in ascending order and degree:  $\chi = [\chi_0^0, \chi_1^{-1}, \chi_1^0, \dots, \chi_L^L]^T$

SH Order, $L$	0	1	2	3	4
# Eigenbeams $\mathcal{L}$	1	4	9	16	25
Approx. Error, $\varepsilon(\%)$	3.82	3.77	3.45	2.74	1.38
Complexity Factor, $\beta$	-	0.002	0.022	0.125	0.477

$\varepsilon(\%)$ : Total squared error between received and  $L$ -th order approximation  
 $\beta = (\frac{\mathcal{L}}{Q})^3$ , where  $Q = 32 \Rightarrow$  More complexity savings with fewer eigenbeams.

## Polynomial Eigenvalue Decomposition (PEVD)

Space-time Covariance Matrix, assuming stationarity, is:

$$\mathbf{R}_{\chi\chi}(\tau) = \mathbb{E}[\chi(n)\chi^H(n-\tau)]$$

Para-Hermitian Polynomial Matrix:

$$\mathcal{R}_{\chi\chi}(z) = \sum_{\tau=-W}^W \mathbf{R}_{\chi\chi}(\tau) z^{-\tau}$$

The PEVD of  $\mathcal{R}_{\chi\chi}(z)$  is [3]:

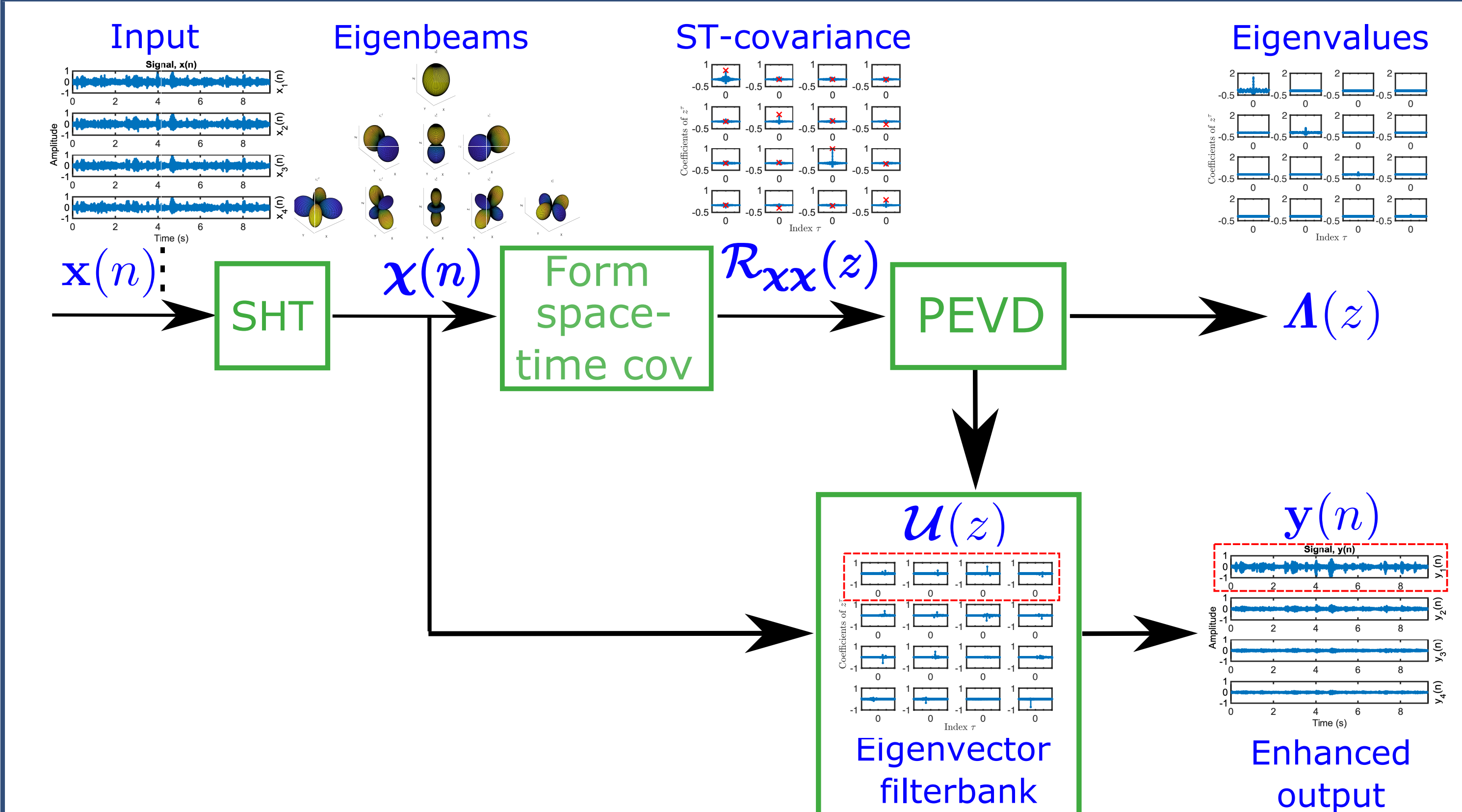
$$\mathcal{R}_{\chi\chi}(z) \approx \mathbf{U}^P(z) \mathbf{\Lambda}(z) \mathbf{U}(z)$$

$$= \begin{bmatrix} \mathbf{U}_s^P(z) & \mathbf{U}_v^P(z) \end{bmatrix} \begin{bmatrix} \mathbf{\Lambda}_s(z) & \mathbf{0} \\ \mathbf{0} & \mathbf{\Lambda}_v(z) \end{bmatrix} \begin{bmatrix} \mathbf{U}_s(z) \\ \mathbf{U}_v(z) \end{bmatrix}$$

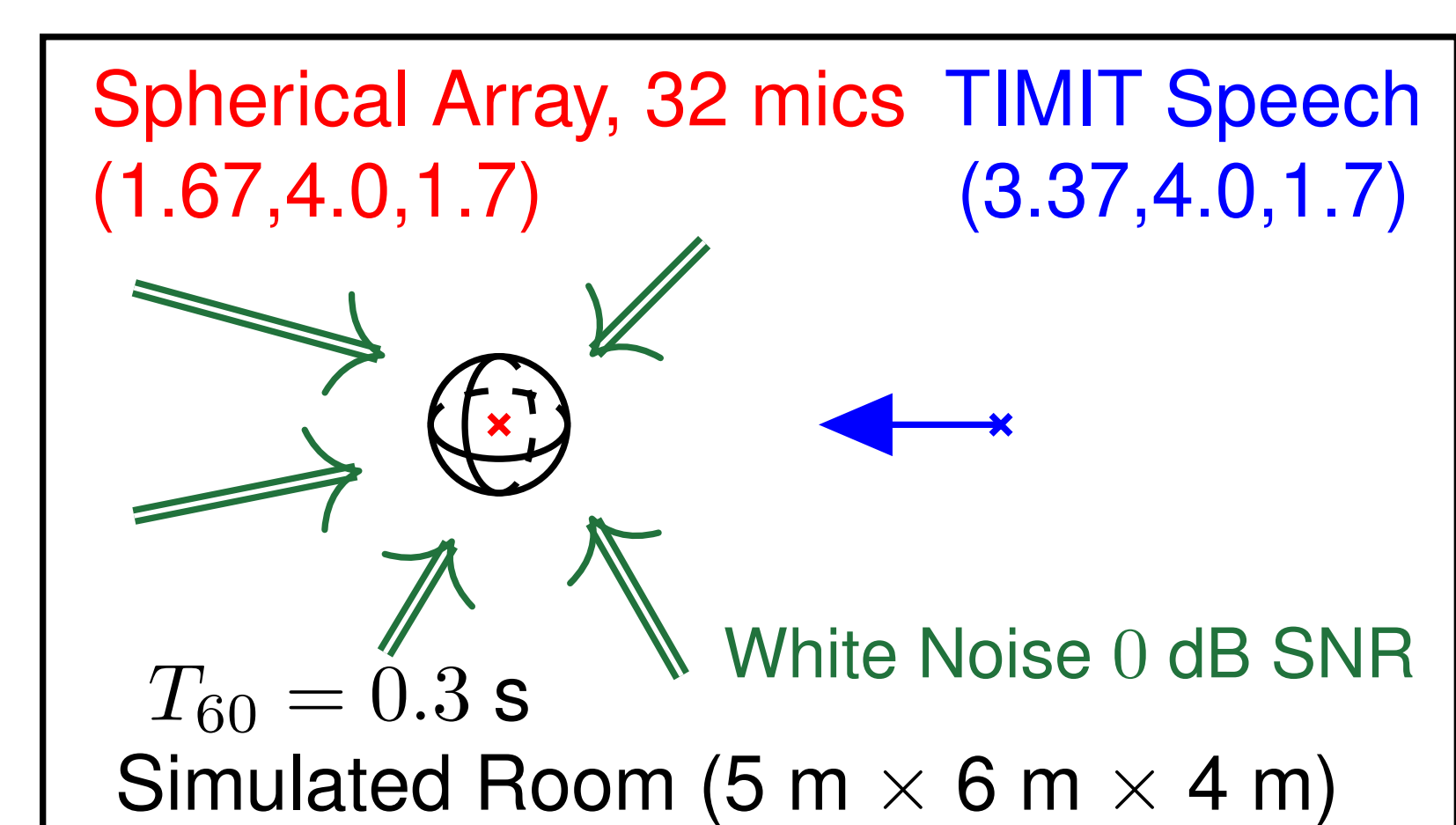
Filtering the eigenbeams through the  $\mathbf{U}(z)$  generates the enhanced signal:

$$\mathbf{y}(z) = \begin{bmatrix} \mathbf{U}_s(z) \\ \mathbf{0} \end{bmatrix} \chi(z)$$

## PEVD of Spherical Harmonics Algorithm



## Experiment Setup: Reverberant Speech in Noise



Comparative algorithms:

1. Eigenbeams  $\chi_0^0, \chi_1^1$
2. KLT $\{\chi_0^0\}$  - Uses an EVD on eigenbeam
3. Raw PEVD - 32 microphone signals for PEVD
4. PEVD L1, L2 - Use SH order 1, 2 eigenbeams  $\Rightarrow$  4, 9 signals for PEVD

Enhancement measures:

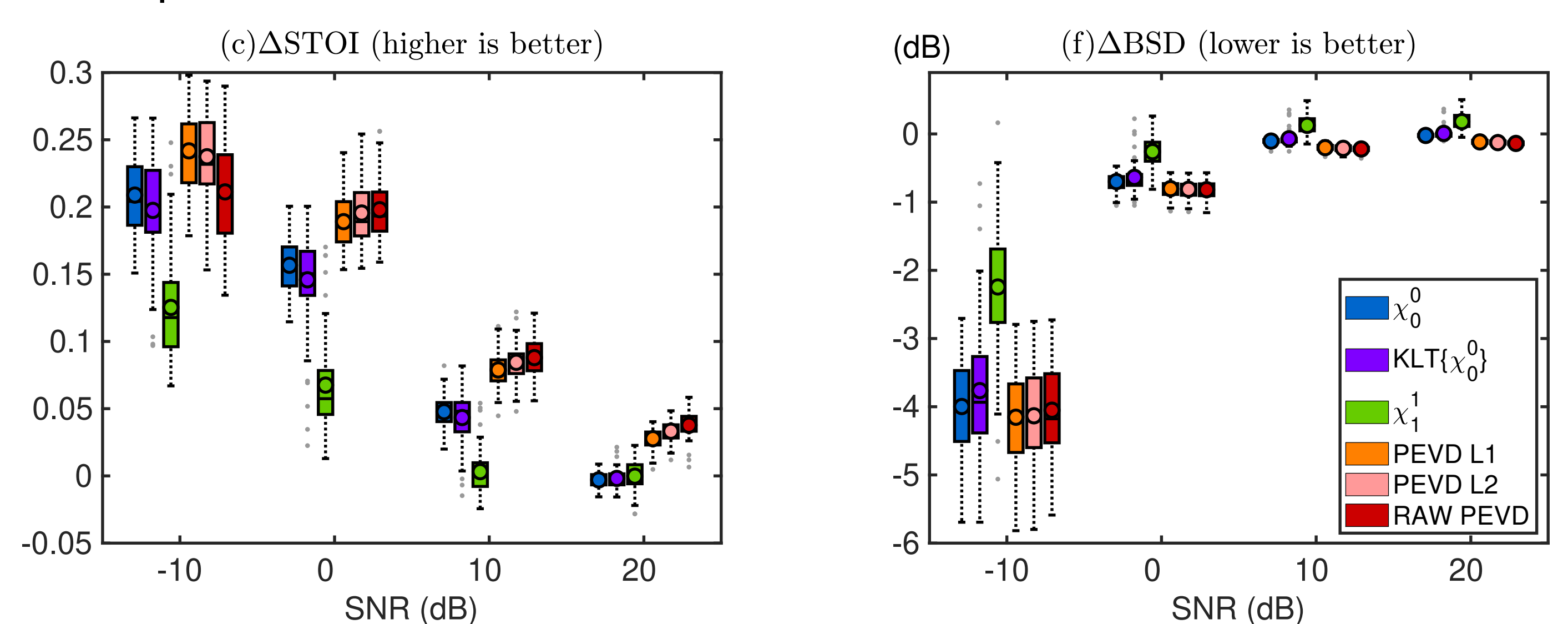
- Frequency-weighted Segmental SNR (FwSegSNR)
- Short-Time Objective Intelligibility (STOI)
- Perceptual Evaluation of Speech Quality (PESQ)
- Bark Spectral Distortion (BSD)

## Speech Enhancement Results

SMIRGen Room, 0 dB White Noise

Algorithm	$\Delta$ FwSegSNR	$\Delta$ STOI	$\Delta$ PESQ	$\Delta$ BSD
$\chi_0^0$	4.86 dB	0.055	0.42	-1.53 dB
KLT $\{\chi_0^0\}$	5.56 dB	0.054	<b>0.51</b>	-1.65 dB
$\chi_1^1$	0.89 dB	0.122	0.44	-0.65 dB
PEVD L1	5.72 dB	0.110	0.47	-1.68 dB
PEVD L2	<b>5.92 dB</b>	<b>0.125</b>	<b>0.51</b>	<b>-1.71 dB</b>
Raw PEVD	5.59 dB	0.119	0.49	-1.62 dB

ACE Corpus: Lecture Room 2, Babble Noise



## References

- [1] V. W. Neo, C. Evers, and P. A. Naylor, "PEVD-based speech enhancement in reverberant environments," in *Proc. IEEE ICASSP*, 2020, pp. 186–190.
- [2] —, *PEVD using spherical harmonics for speech enhancement*, Oct. 2020. [Online]. Available: <https://vwn09.github.io/shd-pevd/>.
- [3] J. G. McWhirter, P. D. Baxter, T. Cooper, S. Redif, and J. Foster, "An EVD algorithm for para-Hermitian polynomial matrices," *IEEE Trans. Signal Process.*, vol. 55, no. 5, pp. 2158–2169, May 2007.